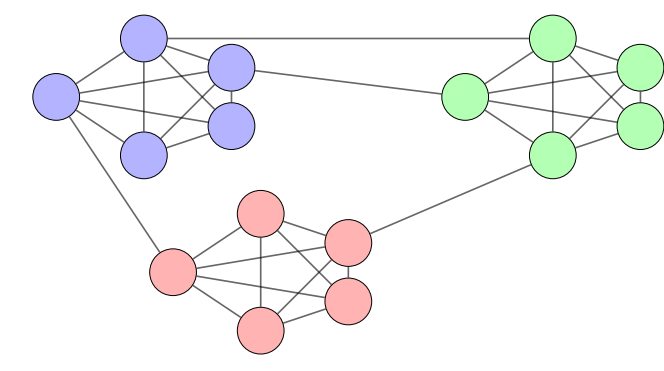
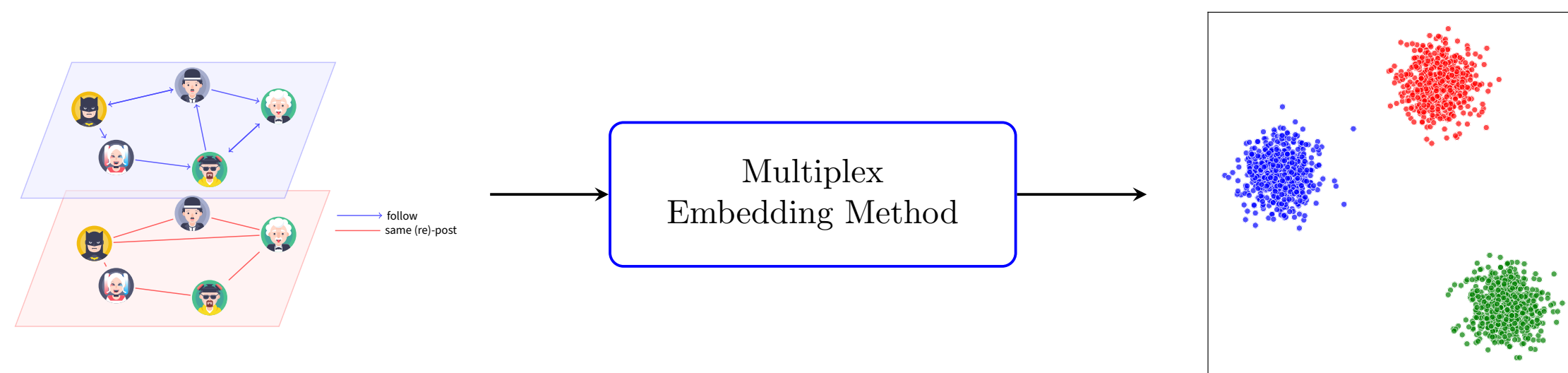


## Context and Motivation

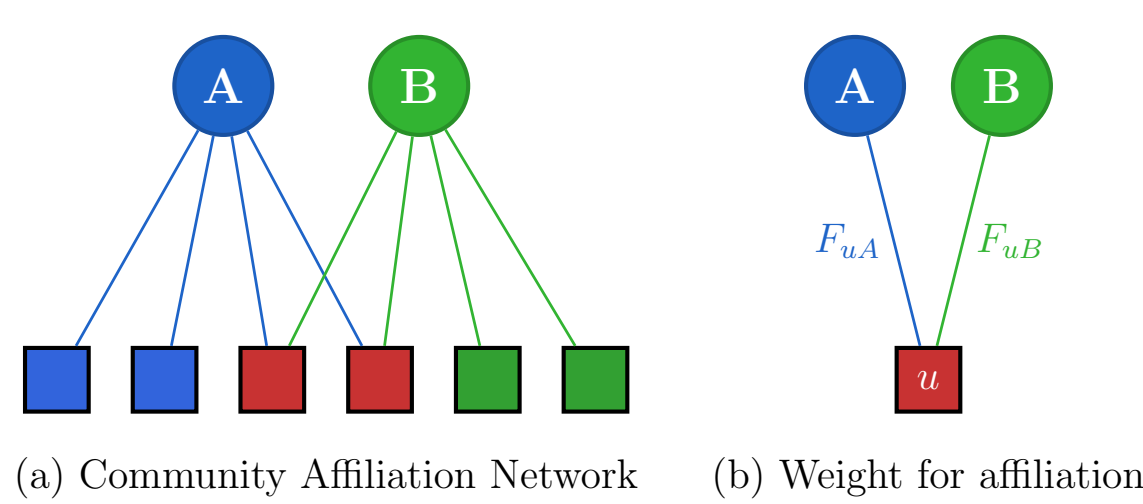
Community detection identifies groups of nodes that are more densely connected to each other than to the rest of the network



- Most existing methods focus on single-layer networks
- However, Online Social Networks (OSNs) are inherently multiplex, with multiple types of interactions (e.g., follows, reposts, likes, etc.) between the same set of users
- Our goal: leverage the multiplex structure of OSNs to embed users in a latent space that **captures their community memberships across all layers**



## Generative Model



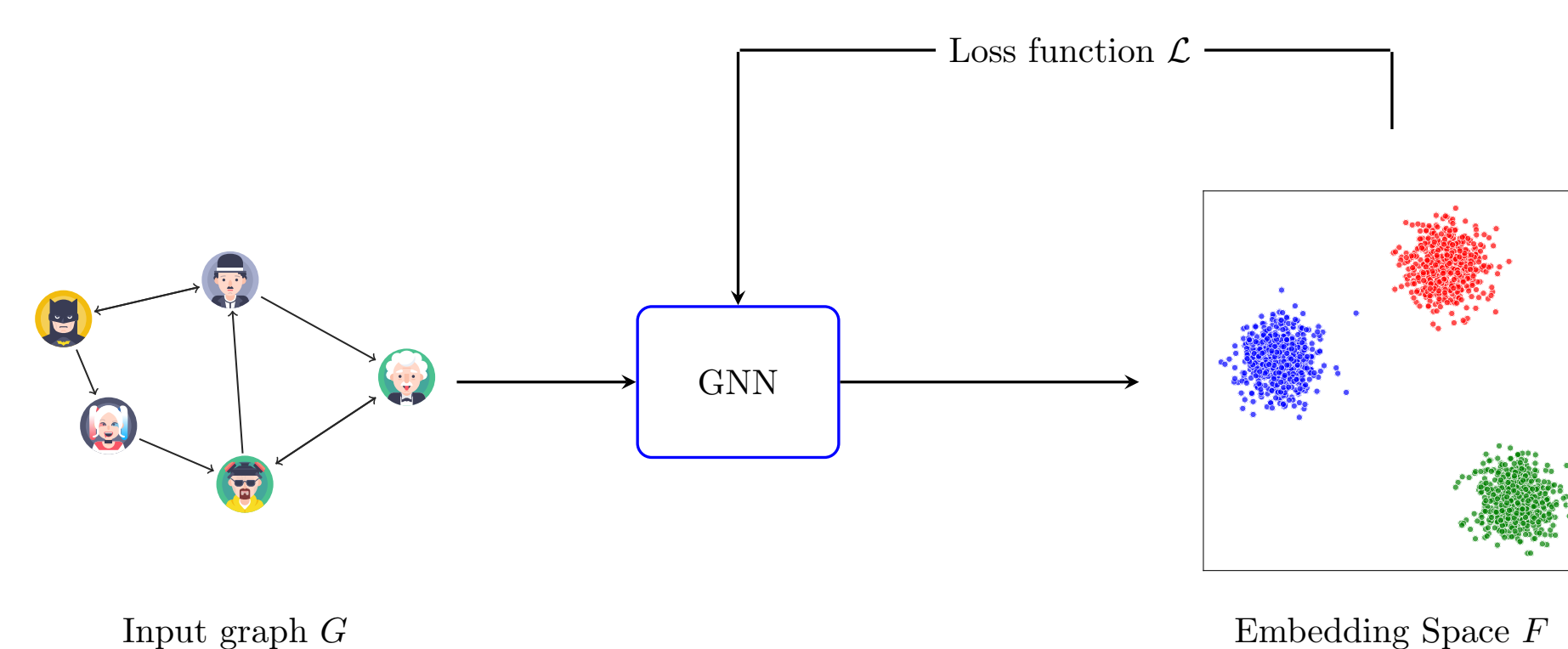
**BigClam** [3] is a generative model for overlapping community detection in **single-layer networks**. It assumes that each node  $u$  has a non-negative affiliation strength  $F_{uc}$  to each community  $c$

- The probability of an edge between nodes  $u$  and  $v$  is given by:

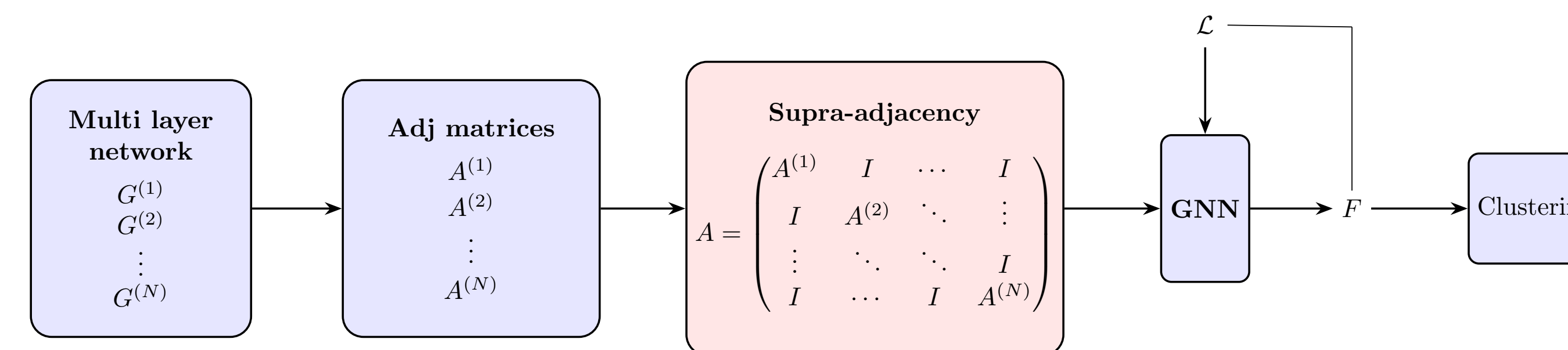
$$P((u, v) \in E | F) = 1 - e^{-F_u^T \cdot F_v}$$

- The model can be trained with a **Graph Neural Network (GNN)** [2] to learn the affiliation matrix  $F$  that best explains the observed network structure. The loss function is the negative log-likelihood of the observed edges:

$$\mathcal{L}(F) = - \sum_{(u,v) \in E} \log(1 - e^{-F_u^T \cdot F_v}) + \sum_{(u,v) \notin E} F_u^T \cdot F_v$$



## Proposed Multiplex Extension



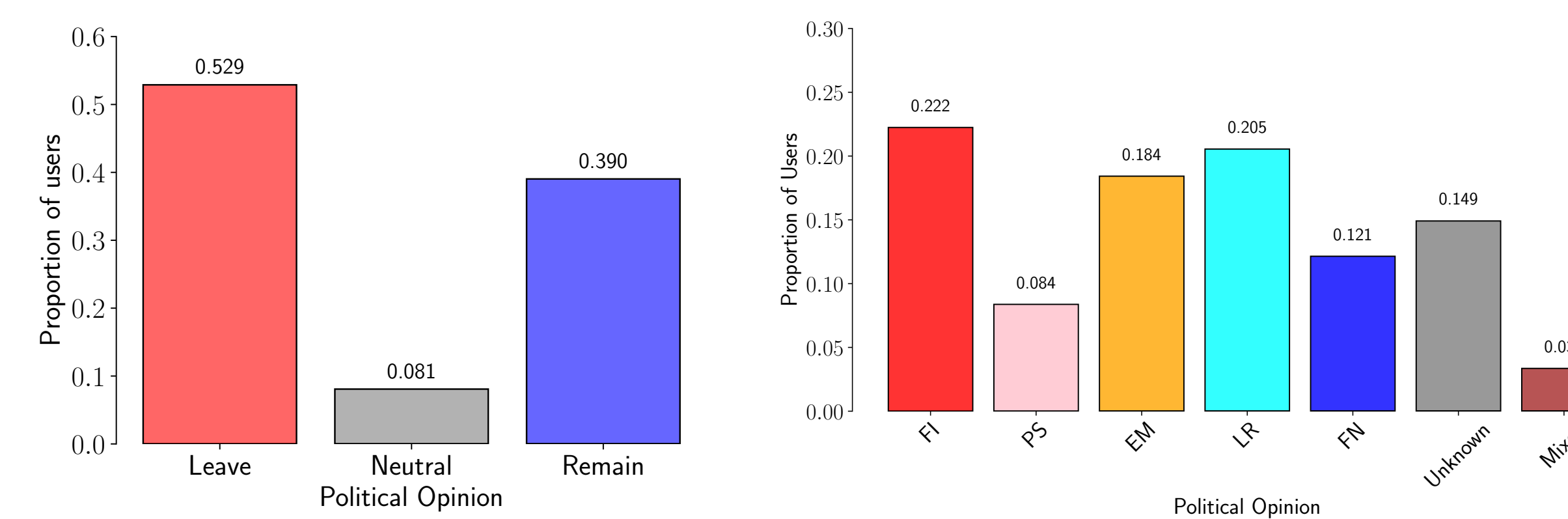
- We build upon the BigClam model by introducing a **multiplex embedding method** that learns a shared affiliation matrix  $F$  across all layers of the multiplex network
- The learning process is done by a GNN on the **supra-adjacency matrix** of the multiplex, which jointly captures intra-layer connections and inter-layer identity links, allowing us to leverage the full multiplex structure for community detection.

## Real World Applications: Polarization in OSNs

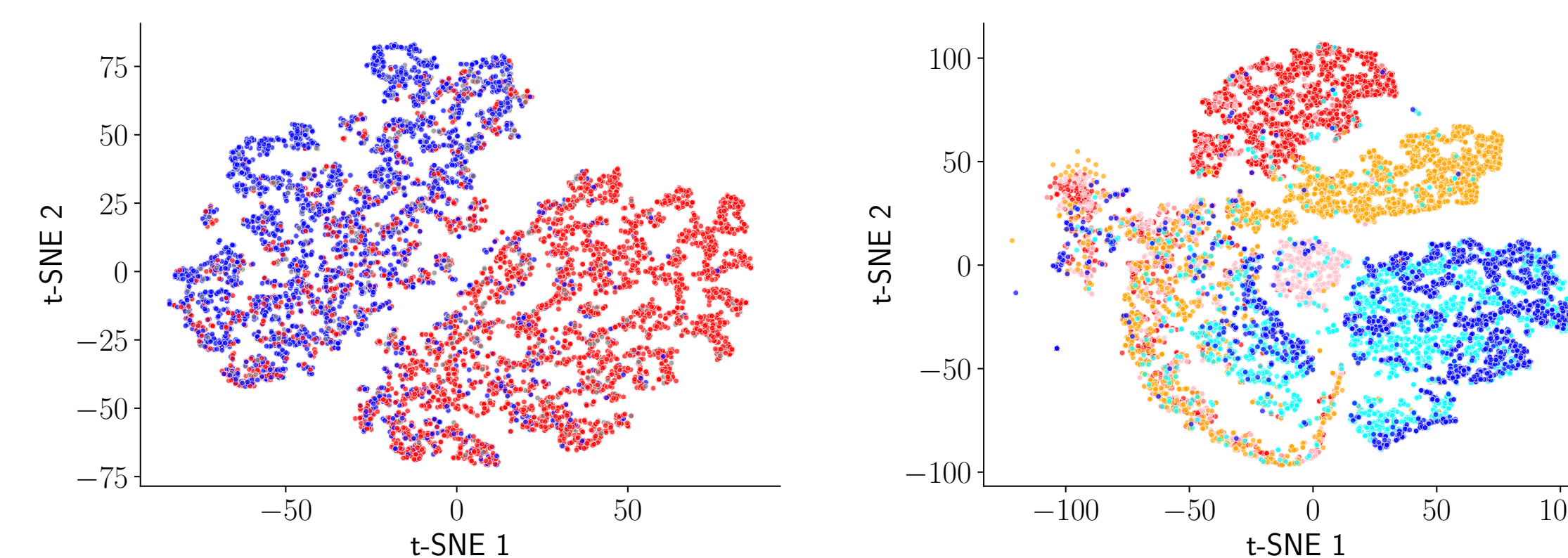
Online discussions on political topics often lead to the formation of polarized communities.

We apply our method to two real-world datasets:

- Brexit**, Twitter debate around the UK referendum on leaving the EU  $|V| \approx 7.59k$  users,  $|E_f| \approx 532k$  follows,  $|E_r| \approx 340k$  reposts.
- Elysée**, Twitter debate around the 2017 French presidential election  $|V| \approx 17.3k$  users,  $|E_f| \approx 2.41M$  follows,  $|E_r| \approx 5.33M$  reposts.



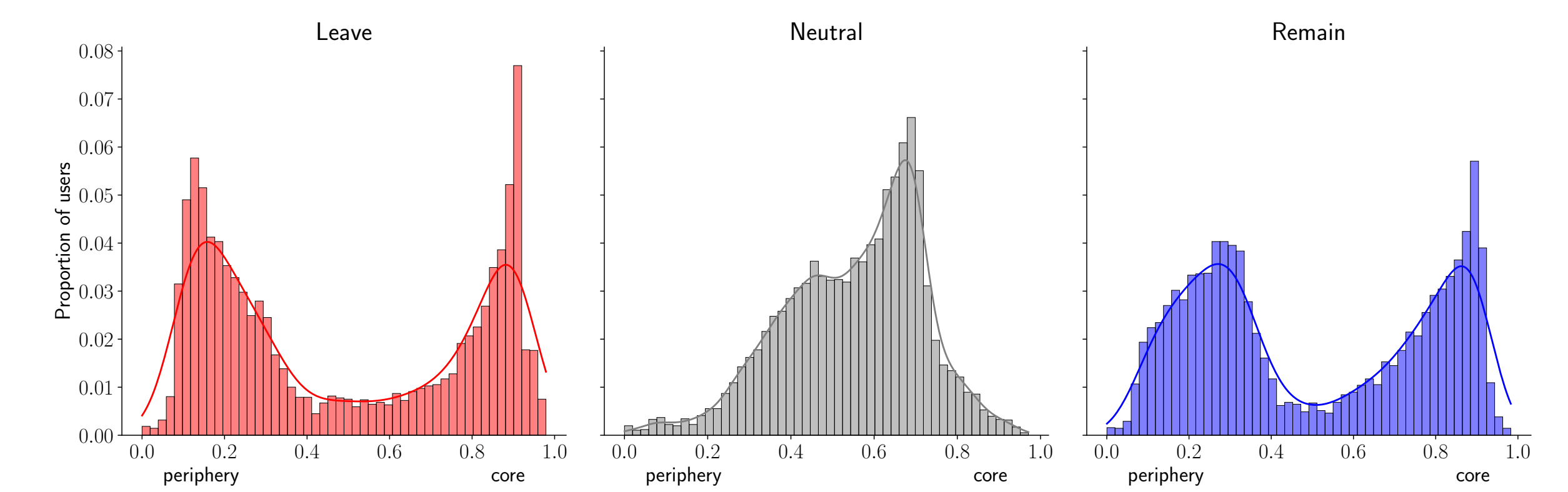
- The **learned embeddings tend to cluster** users with similar political opinions together



- We measure the **reciprocal user diversity** [1] relative to each opinion group centroid, which quantifies how concentrated a user's embedding is around the centroid of a given opinion group:

$$D(\tilde{F}_u || \tilde{F}_o)^{-1} = \left( \sum_{k=1}^K \tilde{F}_{uk}^2 / \tilde{F}_{ok} \right)^{-1}$$

where  $\tilde{F}_u$  is the normalized embedding of the user and  $\tilde{F}_o$  is the normalized centroid of the opinion group.  $K$  is the embedding dimension.



Reciprocal user diversity in Brexit relative to the opinion groups' centroids

- Leave and Remain centroids  $\rightarrow$  clear **bimodal distributions**. Each mode is far from the other, indicating that most users are either close to an opinion centroid or far from it, which implies that the learned embeddings from the multiplex structure effectively capture the polarized community structure in the OSN.
- Neutral centroid  $\rightarrow$  the distribution is skewed towards 0.6, suggesting that neutral users do not form a coherent community in the embedding space, but are instead scattered across the polarized communities.

## Future Work

This work is part of a broader effort to understand **complex interactions** in OSNs. Our goal is to provide multiplex embeddings that capture these interactions and to further analyze the learned embeddings.

By doing so, we aim to uncover the specific multiplex interaction **patterns that define polarized communities** and distinguish them from neutral or less polarized groups.

## References

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